

# Spatial statistics and causal inference:

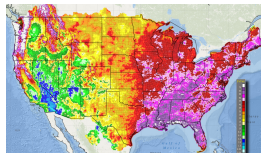
## Spatial confounding and interference in air pollution research

Georgia Papadogeorgou

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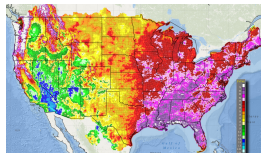
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  - Exposure, outcome, covariates



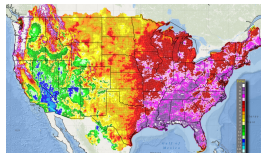
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# Spatial data and causal inference in air pollution research

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  - Exposure, outcome, covariates
- Questions of interest are often causal
  - What is the effect of a specific intervention on polluting sources?
- Integration of spatial data and causal inference
  - Spatial correlation of confounding variables
  - Interference, spillover effects



## NO<sub>x</sub> emission control technologies

- Regulations such as the Clear Air Act enforce stricter rules on emissions
- Power plants follow different compliance strategies
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- Selective Catalytic Reduction (SCR) and Selective Non-Catalytic Reduction (SNCR) are the most effective in reducing NO<sub>x</sub>
- Are SCR/SNCR more effective than alternative strategies in reducing ambient ozone concentrations?

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# Data

- Coal and natural gas power plants during June-August 2004
- $A = 1$  if at least half of facility heat input is used by units with installed SCR/SNCR technologies,  $A = 0$  otherwise
- 152 treated facilities, 321 controls
- $Y$ :  $\text{NO}_x$  emissions / 4<sup>th</sup> maximum ambient ozone concentration
- Covariates: Power plant characteristics, demographics, weather





# Statistical challenges

- Unmeasured spatial confounding
  - Volatile organic compounds and sunlight is necessary for the creation of ozone
  - They may confound the relationship of  $\text{NO}_x$  control strategies and ambient ozone
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# Statistical challenges

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  - Weather and atmospheric covariate information varies spatially
- Interference
  - Pollution travels with the wind
  - “Upwind” pollution sources can affect ambient concentrations in the area surrounding power plants at long distances
  - Discussed in vaccine trials, herd immunity, spillover effects

# Adjusting for Unmeasured Spatial Confounders

# Notation

- For unit  $i$ 
  - Treatment  $A_i \in \{0, 1\}$
  - Potential outcomes  $Y_i(1), Y_i(0)$  (SUTVA)
  - Covariates  $L_i = (L_{i1}, L_{i2}, \dots, L_{ip})$

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- Propensity score matching
  - PS model  $P(A = 1 | L)$
  - Match treated units to controls with similar PS estimates

## Unmeasured spatial confounding

- Confounders  $L = (X, U)$ 
  - $X$  are observed,  $U$  are unobserved
- If  $U$  varies spatially, can we adjust for it?
  - If a matched pair is sufficiently close, the treated and control units will have similar values of  $U$



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- Observed variables  $X$ :
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  - $P(A_i = 1|X_i) = f(X_i) = \text{expit}(X_i^T \beta)$
- Navigate the tradeoff between:
  - 1 Making matches as similar as possible with respect to  $X$
  - 2 Small distance of matched pairs to capture similarity in  $U$

## Distance Adjusted Propensity Score Matching

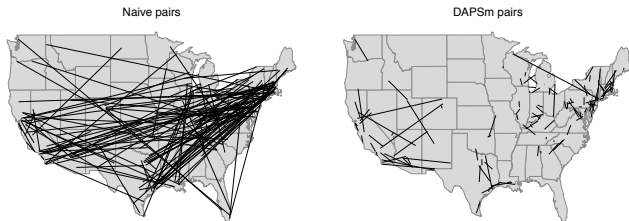
- For a treated unit  $i$  and a control unit  $j$  define

$$DAPSi_j = w|PS_i - PS_j| + (1 - w) * Dist_{ij}, \quad w \in [0, 1]$$

where  $PS$  propensity score estimates, and  $Dist$  spatial proximity.

- $w$ : relative importance of the observed and unobserved confounders
  - High values of  $w$  - most matching weight on observed covariates
  - Low values of  $w$  - most matching weight on spatial proximity

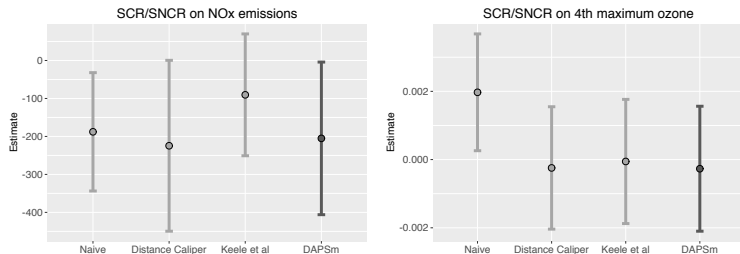
# Matches



- Average distance of matched pairs

- Naïve: 1066 miles
- DAPSm: 141 miles

# Results



- Reduction by 205 tons of NO<sub>x</sub> emissions (95% CI: 4 – 406)
- $-0.27$  (95% CI:  $-2.1$  to  $1.56$ ) parts per billion in ambient ozone

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– The national ambient air quality standard for ozone is 70 parts per billion.  
– Keele et al. [2015]

# Conclusions

- We propose a method to reduce bias from spatial unmeasured confounding
- SCR/SNCR control technologies lead to
  - Reductions in  $\text{NO}_x$  emissions
  - Their effect on ozone is not significant
  
- Additional information in the paper:
  - How to pick the tuning parameter  $w$
  - Robustness to the choice of  $w$  as an indication of no unmeasured spatial confounding
  - Comparison with other methods for incorporating spatial information

## Relaxing the no interference assumption

# Interference

- Previously, we assumed that each unit had  $Y(0), Y(1)$ 
  - *Your* outcome has nothing to do with *my* treatment
- Treatment effects with “interference”
  - *Your* outcome may depend on your and *my* treatment
  - Potential outcomes  $Y(0, 0, \dots, 0), Y(0, 0, \dots, 0, 1)$ , etc



# Interference

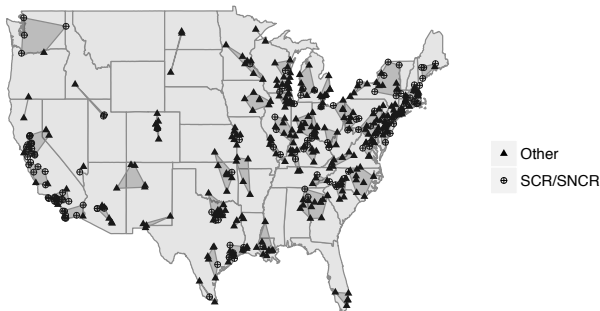
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- Vaccine trials, infectious diseases
- Ambient pollution concentrations are affected by multiple sources
  - Pollution emitted “locally”
  - Pollution that is *transported* from nearby sources

# Partial interference

- *Partial interference*: Partition of units in interference clusters
  - A unit's outcome can depend on the treatment level of units in their cluster
  - Does not depend on treatment of units in other clusters



## Defining estimands in the presence of interference

- Causal inference with interference was introduced in the context of two-stage randomized trials [Hudgens and Halloran, 2008]
- Extensions to observation studies consider estimands for two-stage randomized design (Tchetgen Tchetgen and VanderWeele [2012], Perez-Heydrich et al. [2015])

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- Such estimands represent
  - What would we observe if treatment was assigned randomly to units with probability  $\alpha$ ?
- Are these estimands interpretable?
  - Covariates can be predictors of treatment allocation [Barkley et al., 2017]
  - Dependence between units

# Counterfactual treatment allocation under realistic interventions

- Let  $P_{\alpha,L}$  be the counterfactual treatment allocation
  - How treatment is assigned in a hypothesized world
  - $\alpha$  represents the cluster-average propensity of treatment

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- How would treatment arise in cluster  $i$  if
  - The cluster-average propensity of treatment was set to  $\alpha$ ?
  - Individual treatment adoption depended on a covariate  $L$  with log-odds  $\delta_L$ ?



# Notation

- Clusters  $i \in \{1, 2, \dots, N\}$  with  $n_i$  units
- For unit  $j$  in cluster  $i$ 
  - Treatment  $A_{ij} \in \{0, 1\}$
  - Potential outcomes  $Y_{ij}(\cdot) = \{Y_{ij}(\mathbf{a}_i), \mathbf{a}_i \in \{0, 1\}^{n_i}\}$ ,
  - Unit covariates  $L_{ij} = (L_{ij1}, L_{ij2}, \dots, L_{ijp})$

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- For cluster  $i$ 
  - Cluster treatment  $\mathbf{A}_i = (A_{i1}, A_{i2}, \dots, A_{in_i})$
  - Cluster treatment excluding unit  $j$ :  $\mathbf{A}_{i,-j}$
  - Cluster potential outcomes  $\mathbf{Y}_i(\cdot)$
  - Cluster covariates  $\mathbf{L}_i$

## Covariate dependent counterfactual treatment allocation

How would treatment arise in cluster  $i$  if

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Define

$$\text{logit}P_{\alpha,L}(A_{ij} = 1|L_{ij}; \delta_L) = \xi_i^\alpha + L_{ij}\delta_L$$

where

$$\frac{1}{n_i} \sum_{j=1}^{n_i} P_{\alpha,L}(A_{ij} = 1|L_{ij}; \xi_i^\alpha, \delta_L) = \alpha$$

## Average potential outcome

- Individual average potential outcome

$$\bar{Y}_{ij}(a; \alpha) = \sum_{\mathbf{s}} Y(A_{ij} = a, \mathbf{A}_{i,-j} = \mathbf{s}) P_{\alpha, L}(\mathbf{A}_{i,-j} = \mathbf{s} | A_{ij} = a)$$

Average all possible treatment allocations where

- Observation  $ij$  gets treatment  $a$
- Cluster-level treatment probability is  $\alpha$

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- Group average potential outcome  $\bar{Y}_i(a; \alpha) = \frac{1}{n_i} \sum_{j=1}^{n_i} \bar{Y}_{ij}(a; \alpha)$

- Population average potential outcome  $\bar{Y}(a; \alpha) = E_{G_0}[\bar{Y}_i(a; \alpha)]$ ,  
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for super-population of clusters  $G_0$

- Direct effect for fixed cluster-average treatment propensity

$$DE(\alpha) = \bar{Y}(1, \alpha) - \bar{Y}(0, \alpha)$$

- Indirect effect between two fixed cluster-average treatment propensity

$$IE(\alpha_1, \alpha_2) = \bar{Y}(0, \alpha_1) - \bar{Y}(0, \alpha_2)$$

## Group and population potential outcome estimators

### Assumptions

- **Positivity:**  $P(\mathbf{A}_i = \mathbf{a}_i | \mathbf{L}_i) > 0$ , for all  $\mathbf{a}_i \in \{0, 1\}^{n_i}$
- **Ignorability:**  $\mathbf{Y}_i(\cdot) \perp\!\!\!\perp \mathbf{A}_i | \mathbf{L}_i$



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### Define

$$\hat{Y}_i(a, \alpha) = \sum_{j=1}^{n_i} \frac{P_{\alpha, L}(\mathbf{A}_{i, -j} | A_{ij} = a, \mathbf{L}_i; \boldsymbol{\delta})}{f_{\mathbf{A} | \mathbf{L}, i}(\mathbf{A}_i | \mathbf{L}_i; \boldsymbol{\gamma}) n_i} I(A_{ij} = a) Y_{ij}$$

and

$$\hat{Y}(a; \alpha) = \frac{1}{N} \sum_{i=1}^N \hat{Y}_i(a, \alpha)$$

where  $f_{\mathbf{A} | \mathbf{L}, i}(\mathbf{A}_i | \mathbf{L}_i; \boldsymbol{\gamma})$  is the propensity score of the observed treatment vector

## Theoretical and practical results

- All results assume that positivity and ignorability hold
- $\widehat{Y}_i(a, \alpha)$  is unbiased for  $\overline{Y}_i(a, \alpha)$  (for known propensity score)
- $\widehat{Y}(a; \alpha)$  is consistent (for correctly-specified estimated propensity score)
- Asymptotic results are derived for increasing number of clusters
- Asymptotic or bootstrap CIs are acquired
- Performance was checked in an extensive simulation study
- Coverage of bootstrap CIs was better than asymptotic CIs for a small number of clusters

# Propensity score and counterfactual treatment allocation

- Propensity score of *observed* treatment

$$\text{logit}P(A_{ij} = 1|L_{ij}) = \delta_0 + b_i + L_{ij}^T \boldsymbol{\delta}, \quad b_i \sim N(0, \sigma_b^2)$$

Cluster propensity score:

$$f_{\mathbf{A}|\mathbf{L},i}(\mathbf{A}_i|\mathbf{L}_i; \boldsymbol{\gamma}) = \int \prod_{j=1}^{n_i} P(A_{ij}|L_{ij}, \boldsymbol{\delta}, b_i) f(b_i|\sigma_b^2) db_i$$

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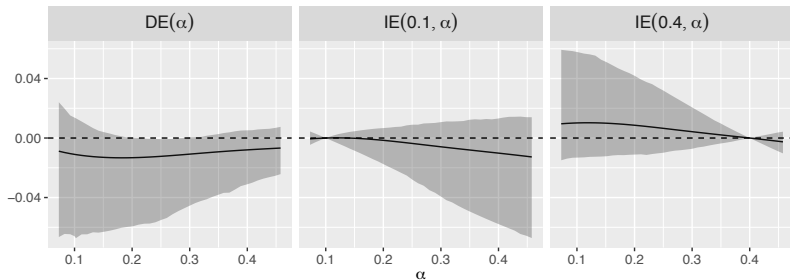
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- Use the observed treatment allocation to inform  $P_{\alpha,L}$

$$\text{logit}P_{\alpha,L}(A_{ij} = 1|L_{ij}; \boldsymbol{\delta}) = \xi_i^\alpha + L_{ij}^T \boldsymbol{\delta}, \quad \text{where}$$

$$\frac{1}{n_i} \sum_{j=1}^{n_i} P_{\alpha,L}(A_{ij} = 1|L_{ij}; \boldsymbol{\delta}) = \alpha$$

## Direct and indirect effect of SCR on ambient ozone



$$DE(\alpha) = \bar{Y}(1, \alpha) - \bar{Y}(0, \alpha)$$

$$IE(\alpha_1, \alpha_2) = \bar{Y}(0, \alpha_1) - \bar{Y}(0, \alpha_2)$$

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Ozone is measured in parts per million

The national ozone air quality standard of 0.07 parts per million.

## Concluding remarks

- Estimands for realistic public health interventions
  - Cluster-average propensity of treatment
  - Distribution of cluster-average propensity of treatment
- Proposed consistent estimators and derived asymptotic variances
- SCR/SNCR technologies are more effective in decreasing ozone against alternatives
  - In the surrounding area
  - In the surrounding area of other power plants

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